

Graphics with MAXIMA

(Version 5.23 and above)

Wilhelm Haager
HTL St. Pölten, Department Electrical Engineering
wilhelm.haager@htlstp.ac.at

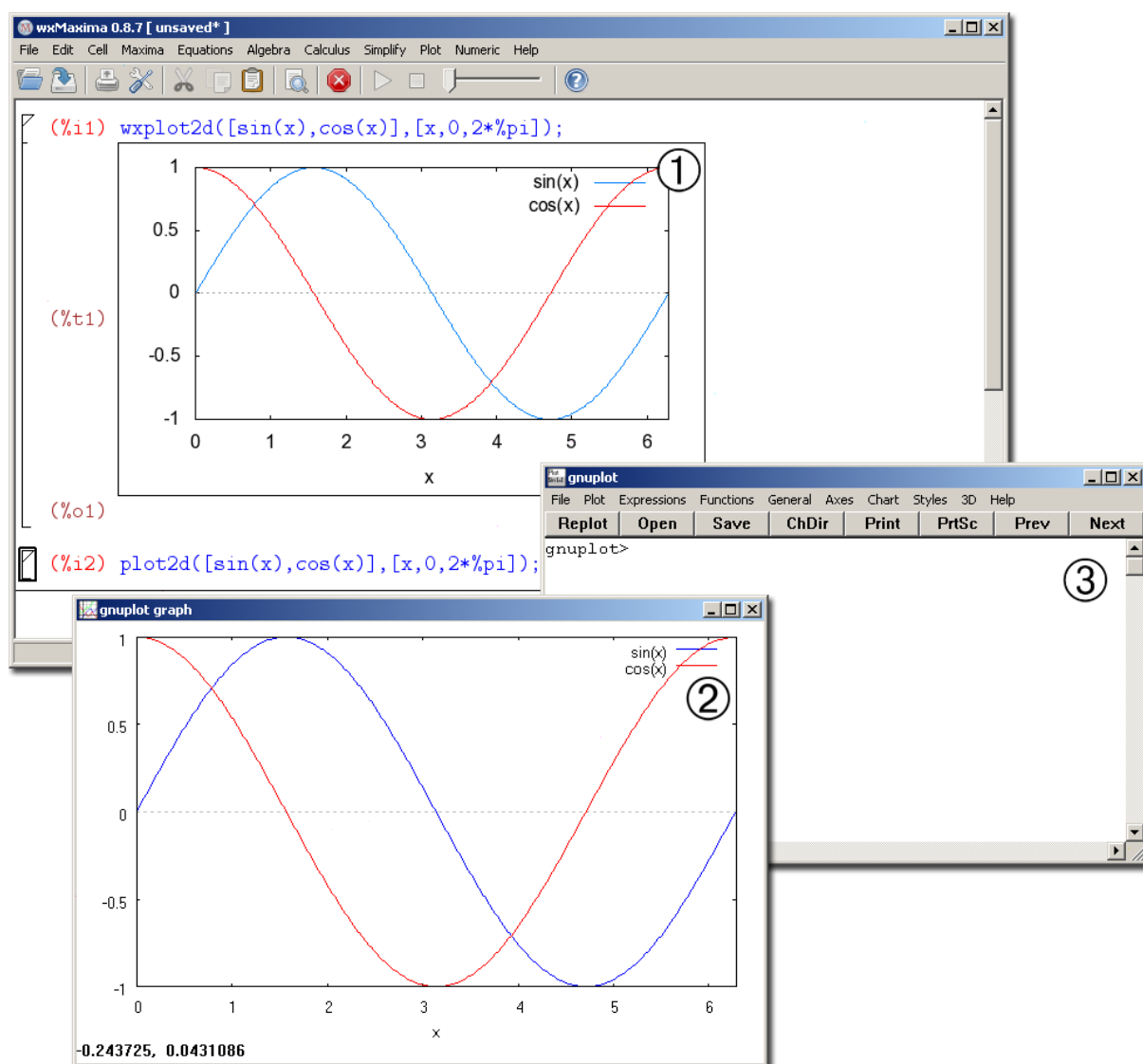
Contents

1	Basics	1
2	Gnuplot	3
2.1	Gnuplot Commands	3
2.2	Gnuplot Terminals	4
2.3	Initialization	5
3	Graphic Interface Plot	6
3.1	Plot Commands	6
3.2	Options	10
4	Graphic Interface Draw	14
4.1	Plot Commands	14
4.2	2d-Graphic Objects	15
4.3	3d-graphic objects	19
4.4	General Options	22
4.5	Options for Labels and Vectors	26
4.6	Options for 2d-Graphics	27
4.7	Options for 3d-Graphics	29
	Bibliography	32

1 Basics

Maxima uses the program *Gnuplot* for depicting graphics [2], which is called automatically, when the graphic is produced. Two various methods for displaying the graphics are possible:

1. When calling the standard plotting routines `plot2d`, `plot3d`, `draw2d`, `draw3d`, etc., a Gnuplot output window containing the graphic is popping up. Continuing working with Maxima is not possible until that window is closed again. The Gnuplot output window and



- ① ... Graphic in wxMaxima working window
- ② ... Graphic in Gnuplot output window
- ③ ... Gnuplot console

consequently the graphic too can be resized using the mouse. Measurements can be performed in 2d-plots with the mouse, 3d-plots can be rotated in any arbitrary direction.

Right-clicking the window title opens a context menu, which enables printing the graphic and opening the Gnuplot console. Using that console window, Gnuplot can be used as a separate program, even independently of Maxima.

2. When preceding the letters “wx” to the names of the plotting routines (`wxplot2d`, `wxplot3d`, `wxdraw2d`, `wxdraw3d`, ...), PNG-graphics are produced in screen resolution and placed directly into the wxMaxima working window. As the graphics remain visible during the entire Maxima session, that method is beneficial for interactive work. Right clicking the graphic enables copying into the clipboard or saving as a file. Nevertheless, due to its low resolution, further use of a graphic produced in that way is not reasonable.

Two various Gnuplot interfaces are available, the Maxima standard functions with the stem “plot” in the function names, as well as the routines of the additional package *Draw* [3] with the stem “draw” in the function names.

The routines of the package *Draw* are admittedly slightly more complicated concerning their usage, but they are more flexible than the standard routines and offer much more possibilities to adapt the graphics with the aid of options to particular requirements. Furthermore it is possible, to set output format (eps, png, jpg, etc.) and output target (i. e. the filename) in the gnuplot console *after* the graphic has been produced, which is apparently not possible when using the standard routines of the Gnuplot interface *Plot*.

2 Gnuplot

Gnuplot is a command-line oriented plot program. When called by Maxima, the input of commands into the Gnuplot console window is not necessary in general, but can be helpful, especially when using the Gnuplot interface *Draw*. For that reason the basic principles and the (few) most important commands of Gnuplot are explained below.

2.1 Gnuplot Commands

<code>plot $f(x)$ <i>opts</i></code>	Plotting the function $f(x)$ with the options <i>opts</i> ; fundamental command for producing graphics, but there is no need for it within Maxima.
<code>replot</code>	Plotting a graphic anew, occasionally with changed settings
<code>set terminal <i>term opts</i></code>	Setting the output format, if necessary, with additional options <i>opts</i> .
<code>set output "<i>filename</i>"</code>	Setting the output target (filename with the appropriate extension)
<code>set size <i>xscale,yscale</i></code>	Scaling the diagram with respect to the size of the entire graphic
<code>set size ratio <i>n</i></code>	Sets the aspect ratio height/width of the diagram
<code>show <i>item</i></code>	Shows the actual value of <i>item</i> .
<code>cd "<i>directory</i>"</code>	Changes the working directory for the output file
<code>pwd</code>	Shows the working directory
<code>load "<i>filename</i>"</code>	Loads a batch of Gnuplot commands from the file <i>filename</i> .
<code>set/unset <i>key</i></code>	Turns the legend on/off
<code>set/unset hidden3d</code>	Turns the visibility of hidden lines in 3d-plots on/off
<code>set/unset grid</code>	Turns the coordinate grid on/off
<code>set cntrparam <i>spez</i></code>	Controls contour lines in a contour-plot
<code>set view <i>rotx rotz scale scaley</i></code>	Sets the view point of 3d-plots
<code>quit</code>	Exiting Gnuplot; not used within Maxima.

Important Gnuplot Commands

Gnuplot commands are input into the Gnuplot console line by line; one line can contain several commands, separated by semicolons. Commands and parameters are separated by spaces, particular coordinates by colons. Coordinate *ranges* have the form $[x_1 : x_2]$.

The basic plot command `plot` is called by Maxima automatically, when a diagram is produced; input of that command by the user does not make sense.

When using the Gnuplot interface *Draw*, an existing graphic can be drawn anew using the command `replot`, if necessary with changed settings, assigned with the command `set` and shown with the command `show`.

`set terminal` (abbreviated `set term`) assigns the file format of the produced graphic. A plethora of formats is available [2], the most important ones are shown in section 2.2 below.

`set output` assigns the output target, i. e. the name of the graphic file. Unless the entire file path is given as the parameter, but only the filename, the file is saved in the current working directory (assigned with `cd`, shown with `pwd`). The file name `stdout` causes the graphic to be drawn into the Gnuplot output window, regardless of the Gnuplot terminal assigned.

The command `set output` should always be performed *after* the eventual command `set terminal`.

The command `set size` does not assign the size of the entire graphic, but the size of the diagram *within* the graphic with respect to its standard size. Values greater than 1 cause clipping parts of the diagram. `set size ratio` assigns the aspect ratio height/width of the diagram, a negative value does not set the ratio of the *lengths* of the axes, but the ratio of their *scales*. Thus for example `set size ratio -1` causes the same scale of the x- and y-axis (and not the same lengths); in that case e. g. a circle remains an undistorted circle.

The command `set cntrparam` sets the number and values of the contour lines in contour-plots in various ways:

```
set cntrparam levels n           ... automatic calculation of n contour lines
set cntrparam discrete z1,z2,... ... assigning particular values for contour lines
set cntrparam incremental z1,dz,z2 ... contour lines ranging from z1 to z2 with an
                                     interval of dz
```

`set view rotx rotz scale scalez` sets the view of 3d-plots. Herein *rotx* is the rotation around the x-axis (starting from vertical view), *rotz* the rotation around the z-axis *scale* a global scale factor and *scalez* an additional scale factor of the z-axis.

The command `load` starts batch processing of Gnuplot commands, which are stored in a textfile.

2.2 Gnuplot Terminals

Most Gnuplot terminals offer additional options, which allow adapting the graphic with respect to resolution, size, color depth, font and font size. Unfortunately the number and the format of those options are not coherent for all terminals, in particular the Gnuplot manual or [2] has to be consulted.

Pixel Formats:

dumb	retro-style ASCII-art graphic
gif	GIF-graphic (suitable for web pages), 8 bit color depth
png	Portable Network Graphics, developed in order to replace GIF, 24 bit color depth
jpeg	JPG-graphic
latex	\LaTeX -code with the <i>picture</i> environment
windows	on-screen display in the Gnuplot output window

Vector Formats:

aifm	Adobe-Illustrator format (file extension .ai)
dxf	AutoCAD drawing interchange format
eepic	\LaTeX code with the extended <i>picture</i> environment (requires the package eepic)
hpgl	Hewlett-Packard Graphics Language for pen-plotters and CNC milling machines
postscript	Postscript graphic (file extension .ps)
postscript eps	Encapsulated Postscript graphic (file extension .eps)
svg	Scalable Vector Graphics

Important Gnuplot terminals

2.3 Initialization

gnuplot.ini	initialization file for graphic settings
wgnuplot.ini	initialization file for Gnuplot settings (i. e. the visual appearance of Gnuplot)
GNUPLOT	environment variable, contains the path name of the initialization files.

Gnuplot-Initialization

Favored standard settings for producing graphics, e. g. the Gnuplot working directory, can be assigned in a file named `gnuplot.ini`. That file can contain any Gnuplot commands, which are performed at starting Gnuplot.

Standard settings for the appearance of Gnuplot itself, e. g. text size and window size of the gnuplot console, are assigned in the file `wgnuplot.ini`. That File is *not* created by the user directly, but via the context menu of of the Gnuplot console.

The directories containing the initialization files `gnuplot.ini` and `wgnuplot.ini` are assigned in the environment variable `GNUPLOT`.

3 Graphic Interface Plot

Plot is the standard Gnuplot interface of Maxima, convenient in its application, but not very flexible regarding the graphics' appearance. Furthermore, the possibilities for producing 3d-graphics are very limited. When using this interface, it is unfortunately *not* possible, to change appearance, output format or output target of a graphic in the Gnuplot console *after* the graphic has been drawn.

3.1 Plot Commands

<code>plot2d(f(x), xrange, opts)</code>	Plots the function $f(x)$ with the options <i>opts</i> within the range <i>xrange</i> ; <i>xrange</i> must be declared.
<code>plot2d([discrete, xwerte, ywerte], opts)</code>	Plots the points with declaration of x-values and y-values in two distinct lists <i>xwerte</i> and <i>ywerte</i> ; the declaration of a range for the x-values is optional.
<code>plot2d([discrete, werte], opts)</code>	Other possibility for plotting points; the points are given in a nested list $[[x1, y1], [x2, y2], \dots]$.
<code>plot2d([parametric, x(t), y(t), trange], opts)</code>	Plots a parametric curve with the parameter t within the range <i>trange</i>
<code>plot3d(f(x,y), xrange, yrange, opts)</code>	Plots a function $f(x,y)$ with the options <i>opts</i> within the ranges <i>xrange</i> and <i>yrange</i>
<code>plot3d([x(u,v), y(u,v), z(u,v)], urange, vrange, opts)</code>	Plots a parametric surface with the parameters u and v within the ranges <i>urange</i> and <i>vrange</i>
<code>contour_plot(f(x,y), xrange, yrange, opts)</code>	Plots contour lines of a function $f(x,y)$ with the options <i>opts</i> within the ranges <i>xrange</i> and <i>yrange</i>
<code>[x, x1, x2]</code>	Declaration of a range for the variable x with the lower bound $x1$ and the upper bound $x2$

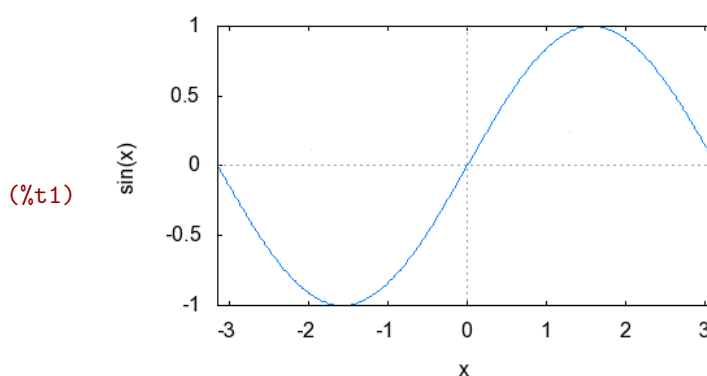
Plot commands of the Gnuplot interface *Plot*

The command `(wx)plot2d` draws a curve or line segments between a couple of points in a two-dimensional cartesian coordinate system. There are three possibilities for that, which can be combined arbitrarily in one single diagram:

1. A function $y = f(x)$; the displayed range along the x-axis must be declared as $[x, x1, x2]$, declaration of y-range is optional.
2. A curve in parametric form $x(t), y(t)$ in dependence of an arbitrarily choosable parameter t . If that parameter has actually the name „t“, the declaration of a range can be omitted. In that case t gets the default values as declared with `set_plot_option`. (the same value for all parametric curves) (section 3.2).
3. Particular points, which can be connected (applying the respective options) by line segments. There are two possibilities for the specification of the points: either in two particular lists containing the x-values and the y-values respectively, or in a single nested list containing the points, each point representing a list containing its x-value and y-value.

Plotting a function within a declared range; the range of the y-axis is calculated automatically.

```
(%i1) wxplot2d(sin(x), [x, -%pi, %pi])$
```



Declaration of x-values in a list:

```
(%i2) xwerte: [0,3,6,4,6,3,0,2,0];
```

```
(%o2) [0,3,6,4,6,3,0,2,0]
```

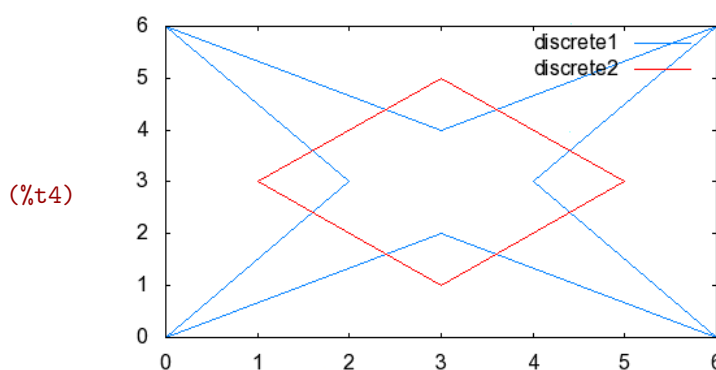
Declaration of y-values in a list:

```
(%i3) ywerte: [0,2,0,3,6,4,6,3,0];
```

```
(%o3) [0,2,0,3,6,4,6,3,0]
```

Two pointwise plots in one diagram with both ways declaring the points. The points are connected by line segments by default.

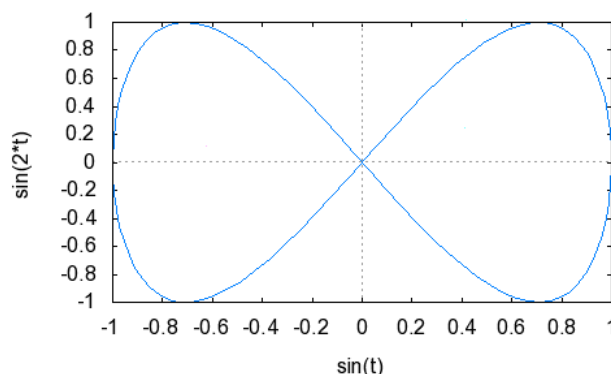
```
(%i4) wxplot2d([[discrete, xwerte, ywerte],  
[discrete, [[3,1], [5,3], [3,5], [1,3], [3,1]]]])$
```



Curve in parametric form; in order to achieve a smooth curve, the number of initial points has to be increased using the option `nticks`.

```
(%i5) wxplot2d([parametric,sin(t),sin(2*t),
[t,0,2*%pi]], [nticks,100])$
```

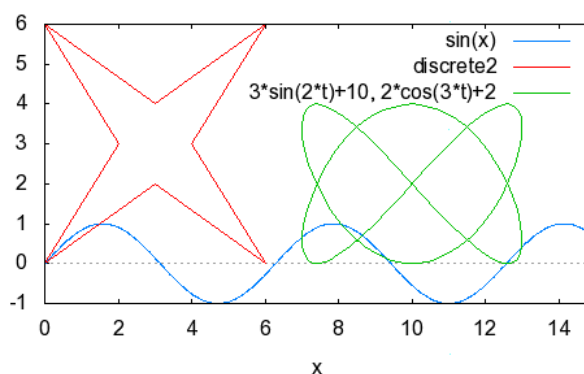
```
(%t5)
```



Combination of three various 2d-plots in one single diagram; the three respective expressions have to be put into a list.

```
(%i6) wxplot2d([sin(x), [discrete,xwerte,ywerte],
[parametric,10+3*sin(2*t),2+2*cos(3*t),
[t,0,2*%pi]]], [x,0,15], [nticks,100])$
```

```
(%t6)
```



One single diagramm can contain any number of curves, put together in a list.

The Gnuplot interface *Plot* offers only very limited possibilities for creating 3d-plots, they are described below only for the sake of completeness. Anyway, the use of the Gnuplot interface *Draw* is recommended for the creation of 3d-graphics.

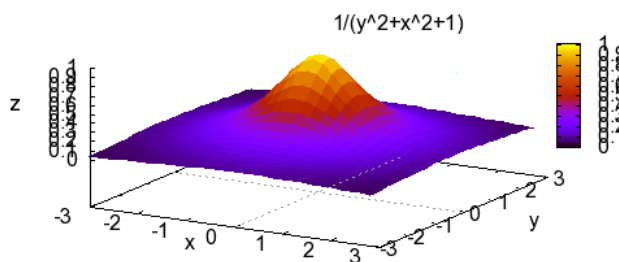
Two kinds of 3d-objects can be produced; however, only one single object can be drawn into a 3d-graphic:

1. A function $z = f(x, y)$; the ranges for x-values and y-values have to be declared. However, the z-range cannot be declared.
2. An object in parametric form $x(u, v), y(u, v), z(u, v)$ in dependence of two (arbitrarily chooseable) parameters u and v . The ranges of the parameters u and v have to be declared, the ranges of the coordinates x, y and z cannot be declared.

3d-plot of a function in two variables; declaration of the ranges for x and y are optional, their default values are stored in the list `plot_options`.

```
(%i7) wxplot3d(1/(1+x^2+y^2), [x, -3, 3], [y, -3, 3])$
```

```
(%t7)
```



Parametric form of a surface in three-dimensional space

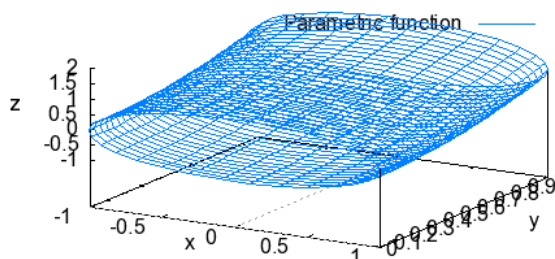
```
(%i8) [fx:cos(x), fy:y, fz:sin(x)+y^2];
```

```
(%o8) [cos(x), y, y^2 + sin(x)]
```

3d-plot of a surface in parametric form

```
(%i9) wxplot3d([fx,fy,fz], [x,0,2*%pi], [y,0,1],  
[palette,false])$
```

```
(%t9)
```

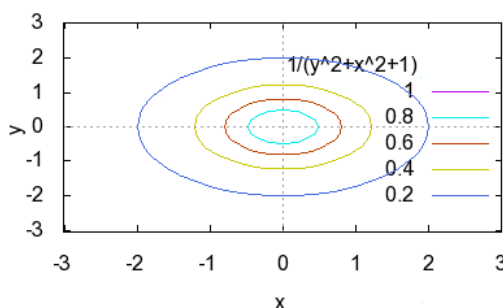


`contour_plot` draws contour lines of a function in two variables within the ranges `xrange` and `yrange`, the number and the values of the contour lines can be declared using the option `gnuplot_preamble` (sections 2.1 und 3.2).

Contour lines of a function in two variables. An explicit declaration of the function values for the lines, as well as turning off the legend, using the appropriate options, would be beneficial.

```
(%i10) wxcontour_plot(1/(1+x^2+y^2),  
[x, -3, 3], [y, -3, 3])$
```

```
(%t10)
```



3.2 Options

Additional optional parameters allow adapting a graphic to particular requirements with respect to colors, line types, sizes, labels, output formats etc. The options are lists (mostly containing two elements); the first element is always the name of the option, additional elements are the associated values.

Options can be stated as additional parameters in every plot command; they can also be declared as default values using the command `set_plot_option`. In that case they are valid for all subsequent plot commands. The command `plot_options` shows all default values of the options.

Commands:

<code>plot_options</code>	Shows all options
<code>set_plot_option([name,v])</code>	Assigns the option <i>name</i> to the value <i>v</i>

Important options:

<code>[y, ymin, ymax]</code>	Range of the y-axis
<code>[x, xmin, xmax]</code>	Range of the x-axis, obligatory in 2d-plots, optional in 3d-plots
<code>[nticks,n]</code>	Number of initial points for calculation of a curve (default:10)
<code>[adapt_depth, n]</code>	Maximum number of curve sections between two initial points (Default:10)
<code>[gnuplot_preamble, "text"]</code>	Gnuplot preamble, contains Gnuplot commands, which precede the plot.
<code>[xlabel, "text"]</code>	x-axis label in 2d-plots
<code>[ylabel, "text"]</code>	y-axis label in 2d-plots
<code>[logx]/[logy]</code>	Logarithmic scaling of the x-/y-axis in 2d-Plots
<code>[legend, "text1", "text2", ...]</code>	Legends for particular curves in a 2d-Plot
<code>[style, style1, style2, ...]</code>	plot styles for the particular curves in a 2d-plot in the form <code>[name,w,c]</code>
<code>[gnuplot_term, terminal]</code>	Output <i>format</i> (i. e. the Gnuplot terminal); ignored by the wx-routines
<code>[gnuplot_out_file, "filename"]</code>	Output <i>target</i> ; ignored by the wx-routines
<code>[grid,nx,ny]</code>	Number of grid lines in 3d-plots in x- and y-direction respectively
<code>[gnuplot_pm3d, true/false]</code>	Controls coloring of surfaces in 3d-plots

Plot options for the Gnuplot interface *Plot*

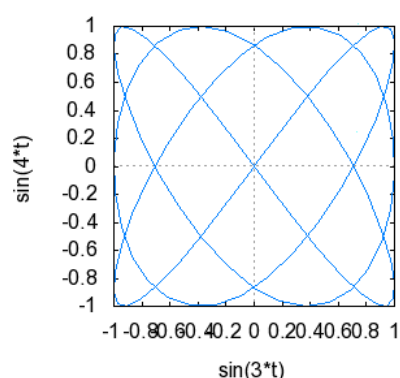
The options `x` and `y` declare the displayed coordinate ranges, in 2d-plots `x` is obligatory. `nticks` and `adapt_depth` set the number and maximum division of initial points for calculating the curve. If the displayed curves are sufficiently “smooth”, its explicit declaration is not necessary.

The option `gnuplot_preamble` can contain any number of Gnuplot commands as a text string, the particular Gnuplot commands are separated by semicolons. They are carried out *prior* the actual plotting process. Hence settings can be passed to Gnuplot, which cannot be controlled by Maxima’s plot options. (e. g. controlling the contour lines in contour plots or setting the aspect ratio of diagrams).

Lissajous curve; the option `gnuplot_preamble` enforces equal scales for both axes, the option `nticks` increases the number of calculated points in order to get a smooth curve.

```
(%i11) wxplot2d([parametric,sin(3*t),sin(4*t),
[t,0,2*pi]], [nticks,100],
[gnuplot_preamble,"set size ratio -1"])$
```

```
(%t11)
```



The option `style` assigns the type of the curve, line width and line color (and the point type, if desired). In pixel graphics the line width is given in pixels, in vector graphics as multiples of 0.25pt (about 0.088mm). The curve type can obtain the following values:

```
lines      ... solid line
points     ... points (with an additional integer number assigning the point type)
linespoints ... solid line and points
impulses  ... bars (line widths and colors are ignored)
```

Colors can have the following values:

```
1 ... blue      2 ... red
3 ... magenta   4 ... yellow
5 ... brown     6 ... green
7 ... cyan
```

List containing x-values

```
(%i12) lx: [1,2,3,4,5,6,7,8,9];
```

```
(%o12) [1,2,3,4,5,6,7,8,9]
```

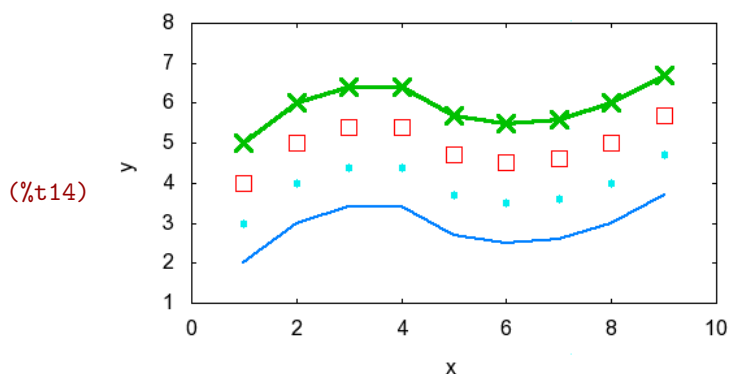
List containing y-values

```
(%i13) ly: [1,2,2.4,2.4,1.7,1.5,1.6,2,2.7];
```

```
(%o13) [1,2,2.4,2.4,1.7,1.5,1.6,2,2.7]
```

Plotting points in various plot styles: as line segments, as points (in various sizes and shapes) and as a combination of both.

```
(%i14) wxplot2d(makelist([discrete,1x,c+ly],c,1,4),
[x,0,10],[y,1,8],[legend,""],
[style,[lines,2,1],[points,2,6,1],
[points,4,2,7],[linespoints,3,4,3]])$
```



(Somewhat tricky) generation of a list of point plots containing one single point each

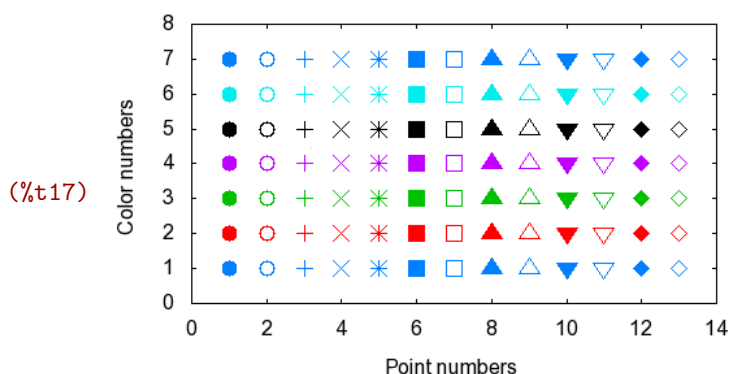
```
(%i15) plotlist:apply(append,makelist(makelist
([discrete,[nx,ny]],nx,1,13),ny,1,7))$
```

(Somewhat tricky) generation of a list of plot styles in all colors and all point types

```
(%i16) stylelist:cons(style,apply(append,makelist(
makelist([points,4,ny,nx],nx,1,13),ny,1,7)))$
```

Plotting all possible colors and point types. Appropriate options suppress the legend and assign labels for the axes.

```
(%i17) wxplot2d(plotlist,stylelist,[x,0,14],[y,0,8],
[legend,""],[xlabel,"Point numbers"],
[ylabel,"Color numbers"])$
```



`gnuplot_term` assigns the output *format*; beside the values `default` and `ps` (for encapsulated postscript) all Gnuplot terminals (section 2.2) are possible. The option `gnuplot_out_file` assigns the output *target* file. Unless the entire file path is given, (inexplicably) *not* the Gnuplot working directory will be used, but the user home directory as declared in the environment variable `HOME`. `gnuplot_term` and `gnuplot_out_file` are ignored by the `wx`-routines.

3d-Plots provide only bare possibilities for changing the settings. The option `gnuplot_preamble` allows assigning settings directly in Gnuplot:

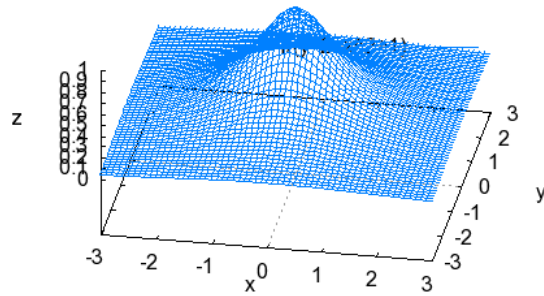
Generation of a Gnuplot preamble for 3d-plots in order to show hidden lines and change the view point

```
(%i18) p:"unset hidden3d;set view 20,10,1,3";
(%o18) unset hidden3d;set view 20,10,1,3
```

3d-plot with a Gnuplot preamble, changes number of grid lines and turned-off color palette

```
(%i19) wxplot3d(1/(1+x^2+y^2), [x,-3,3], [y,-3,3],  
[grid,60,60],[gnuplot_preamble, p],  
[palette,false])$
```

```
(%t19)
```



4 Graphic Interface Draw

The Gnuplot interface *Draw* by Mario Rodríguez Riotorto [3] provides an additional set of Maxima graphic routines, which differ from the standard routines with regard to their parameters, in particular the structure of the options.

The application of these routines, all having the stem “draw” in their function names, is slightly more complicated than of the standard routines. However, they offer much more flexibility for configuration and adapting the graphics to particular requirements. Moreover, output format and output target can be assigned *after* the graphic has been drawn into the Gnuplot output window.

The package *Draw* has to be loaded prior to its first use.

4.1 Plot Commands

<code>draw(scene1, scene2, ..., opts, ...)</code>	Creation of a graphic as a compilation of <i>Szenen</i> and global options <i>opts</i> .
<code>gr2d(opts, graphic_object, ...)</code>	Creation of a 2d- <i>scene</i> as a compilation of arbitrary 2d graphic objects with the options <i>opts</i>
<code>gr3d(opts, graphic_object, ...)</code>	Creation of a 3d- <i>scene</i> as a compilation of arbitrary 3d graphic objects with the options <i>opts</i>
<code>draw2d(opts, graphic_object, ...)</code>	Creation of a 2d-graphic as a compilation of arbitrary 2d graphic objects with the options <i>opts</i>
<code>draw3d(opts, graphic_object, ...)</code>	Creation of a 2d-graphic as a compilation of arbitrary 2d graphic objects with the options <i>opts</i>
<i>Options:</i>	
<code>name1=value1, name2=value2, ...</code>	

Plot commands of the Gnuplot interface *Draw*

A graphic consists of particular (2d- and 3d-) *scenes*, which are output by the basic plot command `draw` in a rectangle array, each scene containing a single diagram.

A scene, a compilation of several *graphic objects* and (if desired) additional *options*, is created with the commands `gr2d` (for 2d-graphics) and `gr3d` (for 3d-graphics).

Most graphics contain only one single diagram (i. e. only one single scene). In that case the plot commands `draw2d` and `draw3d` compile the graphic objects to a scene and draw the graphic for that scene in one single step. Thus the commands

```
draw2d(...) and draw3d(...)
```

are equal to

```
draw(gr2d(...)) and draw(gr3d(...)).
```

The parameter list contains any number of graphic objects and options. Options referring to a particular graphic object must *precede* that object. The position of *global* parameters (e. g. for declaring output format and output target) is arbitrary.

Options are declared as *equations* with its name on the left hand side and its value on the right hand side. The value can also be a *list* (e. g. for assigning ranges with lower bound and upper bound).

At complex graphics containing many objects, the parameter list can get long and somewhat confusing. In that case it is good style, either

- to structure the input by appropriate line breaks and indentations, or (even better)
- not to declare the graphic objects directly in the parameter list of the plot commands, but assign variable names to them in separate commands and use those variable names in the parameter list of the plot commands.

4.2 2d-Graphic Objects

`explicit`, `parametric` and `implicit` create graphic objects from mathematical expressions in cartesian coordinates. `polar` creates a graphic object of a function in polar coordinates. As the displayed ranges are an inherent part of the graphic objects, they need not be declared—contrary to the Gnuplot interface *Plot*—as options.

Furthermore, a number of geometric shapes is available, which allow the composition of arbitrary graphics. The graphic object `points` primarily displays a number of discrete points. Applying the appropriate options, those points can be connected by line segments. Thus `points` enables the creation of any graphic consisting of lines and approximate curves (section 4.4).

<code>explicit($f(x)$, x, $x1$, $x2$)</code>	Function $f(x)$ within the range of $x1$ and $x2$
<code>parametric($x(t)$, $y(t)$, t, $t1$, $t2$)</code>	Parametric curve $x(t), y(t)$ with the parameter t ranging from $t1$ to $t2$
<code>implicit($equation$, x, $x1$, $x2$, y, $y1$, $y2$)</code>	Implicit curve, declared by the equation $equation$, with the variables x and y within the ranges $x1 \dots x2$ and $y1 \dots y2$
<code>polar($r(\varphi)$, φ, $\varphi1$, $\varphi2$)</code>	Function in polar coordinates; radius r with respect to the angle φ in degree ranging from $\varphi1$ to $\varphi2$
<code>points($xvals$, $yvals$)</code>	Points; $xvals$ and $yvals$ are lists containing the x- and y-values respectively
<code>points($p1$, $p2$, ...)</code>	Points; each point pi is a list with its coordinates: $[px, py]$.
<code>polygon($xvals$, $yvals$)</code>	Polygon with declaration of its vertexes in lists $xvals$ and $yvals$.
<code>polygon($p1$, $p2$, ...)</code>	Polygon; each vertex pi is a list containing its coordinates: $[px, py]$.
<code>rectangle($p1$, $p2$)</code>	Rectangle with the opposite vertexes $p1$ and $p2$ in the form $[px, py]$
<code>ellipse($x0$, $y0$, a, b, $w1$, $w2$)</code>	Ellipse (oder circle) with the center $[x0, y0]$, the half-axes a and b , as well as starting angle $w1$ and final angle $w2$
<code>label(["text", x, y], ...)</code>	Label $text$ at the position $[x, y]$; alignment and orientation can be set using options.
<code>vector($[x, y]$, $[dx, dy]$)</code>	Vector with the origin $[x, y]$ and the coordinates $[dx, dy]$
<code>image(m, x, y, nx, ny)</code>	Image object with the matrix m containing $nx \times nx$ pixels and the coordinates $[x, y]$ of the lower left corner

2d graphic objects

Loading the package *Draw*

```
(%i20) load(draw);
(%o20) C:/Programme/Maxima-5.23.2/share/maxima/...
```

Declaring a function $y=f(x)$ as a graphic object

```
(%i21) g1:explicit(2*sin(x), x, -%pi, %pi);
(%o21) explicit(2 sin(x), x, -pi, pi)
```

Parametric curve as graphic object

```
(%i22) g2:parametric(2*sin(phi), 2*cos(phi), phi, 0, 2*%pi);
(%o22) parametric(2 sin(phi), 2 cos(phi), phi, 0, 2 pi)
```

Implicit function as graphic object

```
(%i23) g3:implicit(x^2-y^2=1, x, -4, 4, y, -4, 4);
(%o23) implicit(x^2 - y^2 = 1, x, -4, 4, y, -4, 4)
```

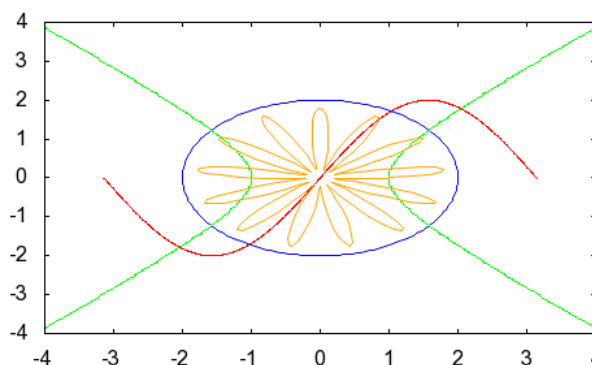
Function $r=f(\varphi)$ in polar coordinates as graphic object

```
(%i24) g4:polar(1+0.8*sin(13*t), t, 0, 2*%pi);
(%o24) polar(0.8 sin(13 t) + 1, t, 0, 2 pi)
```

Plot all graphic objects into one single diagram; using the appropriate options, smooth curves are obtained and the diagram gets some color.

```
(%i25) wxdraw2d(nticks=200,color=red,g1,color=blue,g2,
               color=green,g3,color=orange,g4)$
```

```
(%t25)
```



Polygon as graphic object from lists containing the x-values and y-values each

```
(%i26) poly:polygon(xwerte+2,ywerte+2);
```

```
(%o26) polygon([2,5,8,6,8,5,2,4,2],[2,4,2,5,8,6,8,5,2])
```

“Points”-object from lists containing the x-values and y-values each

```
(%i27) punkte:points([1,3,5,7,9,9,9,9,9,7,5,3,1,1,1,1],
                    [1,1,1,1,1,3,5,7,9,9,9,9,9,7,5,3]);
```

```
(%o27) points([1,3,5,7,9,9,9,9,9,7,5,3,1,1,1,1],
              [1,1,1,1,1,3,5,7,9,9,9,9,9,7,5,3])
```

Declaring a rectangle by its opposite vertexes

```
(%i28) rechteck:rectangle([1,-2],[6,-7]);
```

```
(%o28) rectangle([1,-2],[6,-7])
```

Ellipse as graphic object

```
(%i29) ell:ellipse(6,-6,3,2,0,360);
```

```
(%o29) ellipse(6,-6,3,2,0,360)
```

Bar chart as graphic object

```
(%i30) balken:bars([-7,2,1],[-5,5,1],[-3,7,1],[-1,6,1]);
```

```
(%o30) bars([-7,2,1],[-5,5,1],[-3,7,1],[-1,6,1])
```

Three vectors as graphic objects

```
(%i31) [v1,v2,v3]:[vector([-8,-8],[6,0]),
                 vector([-8,-8],[6,6]),vector([-2,-8],[0,6])];
```

```
(%o31) [vector([-8,-8],[6,0]),vector([-8,-8],[6,6]),
        vector([-2,-8],[0,6])]
```

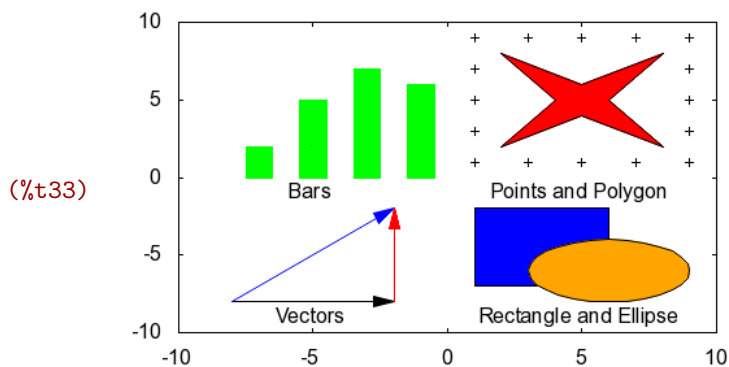
Textstrings as graphic object “label”; all texts are put together in one single object.

```
(%i32) text:label(["Bars",-5,-1],
                 ["Points and Polygon",5,-1],
                 ["Vectors",-5,-9],
                 ["Rectangle and Ellipse",5,-9]);
```

```
(%o32) label([Bars,-5,-1],[Points and Polygon,5,-1],
             [Vectors,-5,-9],[Rectangle and Ellipse,5,-9])
```

Drawing all graphic objects into a single diagram; appropriate options are applied for assigning colors and the shape of the arrowheads.

```
(%i33) wxdraw2d(xrange=[-10,10],yrange=[-10,10],
               punkte,poly,
               fill_color=blue,rechteck,
               fill_color=orange,ell,
               fill_color=green,balken,
               head_length=0.8,head_angle=15,v1,
               color=blue,v2,color=red,v3,
               color=black,text)$
```



`image` generates an image object consisting of quadratic areas representing the particular pixels. Color values can be declared in two ways:

- If the matrix elements are lists containing three numbers, those numbers represent red, green and blue color components of the pixels respectively. Herein those names do *not* represent their *absolute* color values, but color values *relative* to the maximum value which represents full saturation!
- If the matrix elements are single numbers, they are interpreted according to the color palette, assigned with the option `palette`.

Matrix containing color values according to the standard color palette

```
(%i34) m1:matrix([0,50,100],[50,100,150],[100,150,200]);
```

```
(%o34) 
$$\begin{pmatrix} 0 & 50 & 100 \\ 50 & 100 & 150 \\ 100 & 150 & 200 \end{pmatrix}$$

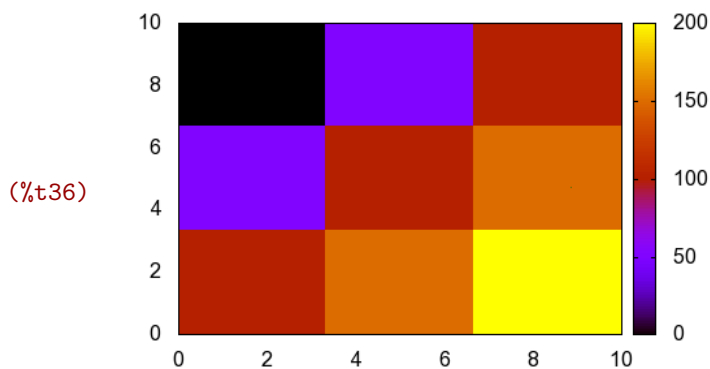
```

Generation of an image object

```
(%i35) im1:image(m1,0,0,10,10)$
```

Drawing that image object

```
(%i36) wxdraw2d(im1)$
```



With the use of the additional package `picture`, which is loaded automatically with `Draw`, Maxima gets some (very limited) possibilities for image processing: Image objects can be loaded from

XPM-files, color channels can be extracted from images, images can be composed from color channels [1], [3].

4.3 3d-graphic objects

<code>explicit($f(x,y)$, x, $x1$, $x2$, y, $y1$, $y2$)</code>	Function $f(x,y)$ within the ranges $x1 \dots x2$ and $y1 \dots y2$
<code>implicit($equation$, x, $x1$, $x2$, y, $y1$, $y2$, z, $z1$, $z2$)</code>	Implicit curve defined by $equation$, in the variables x , y and z within the ranges $x1 \dots x2$, $y1 \dots y2$, $z1 \dots z2$
<code>parametric($x(t)$, $y(t)$, $z(t)$, t, $t1$, $t2$)</code>	Parametric curve $x(t), y(t), z(t)$ with the parameter t ranging from $t1$ to $t2$
<code>parametric_surface($x(u,v)$, $y(u,v)$, $z(u,v)$, u, $u1$, $u2$, v, $v1$, $v2$)</code>	Parametric surface $x(u,v), y(u,v), z(u,v)$ with the parameters u and v within the ranges $u1 \dots u2$ and $v1 \dots v2$
<code>cylindrical($r(z,\varphi)$, z, $z1$, $z2$, φ, $\varphi1$, $\varphi2$)</code>	Surface in cylindric coordinates; radius $r(z,\varphi)$ with respect to the z -coordinate z ranging from $z1$ to $z2$ and azimuth φ ranging from $\varphi1$ to $\varphi2$
<code>spherical($r(\varphi,\vartheta)$, φ, $\varphi1$, $\varphi2$, ϑ, $\vartheta1$, $\vartheta2$)</code>	Surface in spherical coordinates; radius $r(\varphi,\vartheta)$ with respect to the azimuth φ ranging from $\varphi1$ to $\varphi2$ and the zenith ϑ ranging from $\vartheta1$ to $\vartheta2$
<code>points($xvals$, $yvals$, $zvals$)</code>	Points; $xvals$, $yvals$ and $zvals$ are lists containing the x -, y - and z -values respectively
<code>points($p1$, $p2$, ...)</code>	Points; each point pi is a list containing its coordinates: $[px, py, pz]$.
<code>label(["text", x, y, z], ...)</code>	Text label $text$ at the position $[x,y,z]$; alignment, font etc. can be set using options.
<code>vector($[x,y,z]$, $[dx,dy,dz]$)</code>	Vector with the origin $[x,y,z]$ and its coordinates $[dx,dy,dz]$

3d-graphic objects

`explicit` and `implicit` define graphic objects by mathematical expressions in cartesian coordinates as surfaces in three-dimensional space. `parametric` defines a parametric curve with the parameter t , `parametric_surface` defines a surface in parametric form with two parameters u and v . `cylindrical` and `spherical` define a surface in cylindric and spheric coordinates respectively.

Contrary to the Gnuplot interface `Plot`, one single diagramm can contain any number of graphic objects.

Sphere, defined as an implicit function

```
(%i37) gimp:implicit(1=x**2+y**2+z**2,
                    x,-1,1,y,-1,1,z,-1,1);
```

```
(%o37) implicit(1 = z2 + y2 + x2, x, -1, 1, y, -1, 1, z, -1, 1)
```

Two-dimensional function

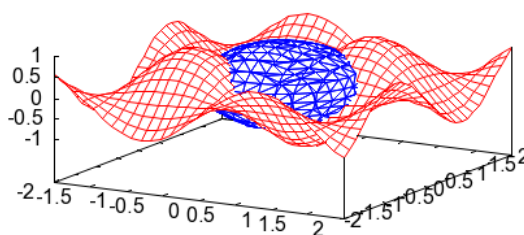
```
(%i38) gexp:explicit(sin(2*x)*sin(2*y), x, -2, 2, y, -2, 2);
```

```
(%o38) explicit(sin(2 x) sin(2 y), x, -2, 2, y, -2, 2)
```

Drawing the sphere and the two-dimensional function into one diagram. The option `surface_hide` suppresses hidden parts.

```
(%i39) wxdraw3d(surface_hide=true,
                 color=red,gexp,color=blue,gimp)$
```

(%t39)



Toroidal spiral as parametric curve with four windings around a toroid

```
(%i40) spiral:parametric((2-0.5*cos(t))*sin(t/4),
                          (2-0.5*cos(t))*cos(t/4),
                          0.5*sin(t), t, 0, 8*pi);
```

```
(%o40) parametric(sin(t/4) (2 - 0.5 cos(t)),
                  cos(t/4) (2 - 0.5 cos(t)),
                  0.5 sin(t), t, 0, 8 pi)
```

Toroid as 3d-surface in parametric form

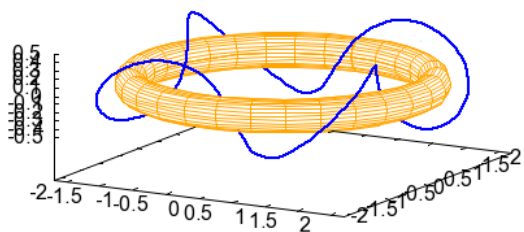
```
(%i41) torus:parametric_surface(
        (2-0.2*cos(phi))*sin(theta),
        (2-0.2*cos(phi))*cos(theta),
        0.2*sin(phi), phi, 0, 2*pi, theta, 0, 2*pi);
```

```
(%o41) parametric_surface((2 - 0.2 cos(phi)) sin(theta),
                          (2 - 0.2 cos(phi)) cos(theta), 0.2 sin(phi),
                          phi, 0, 2 pi, theta, 0, 2 pi)
```

Common display of toroid and spiral

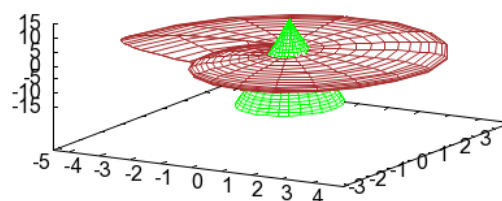
```
(%i42) wxdraw3d(nticks=200,surface_hide=true,
                 color=orange,torus,
                 line_width=2,color=blue,spiral)$
```

(%t42)



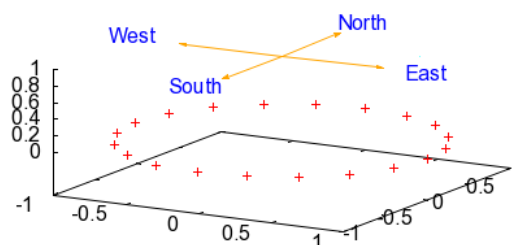
Cone as a function in cylindric coordinates	(%i43) <code>cone:cylindrical((z-15)*0.05,z,-15,15,phi,0,2*%pi);</code>
	(%o43) <code>cylindrical(0.05(z-15),z,-15,15,φ,0,2π)</code>
Snail shell like surface, defined in spheric coordinates	(%i44) <code>snail:spherical(4+0.5*phi,phi, -2*%pi,%pi,tht,0,%pi);</code>
	(%o44) <code>spherical(0.5φ+4,φ,-2π,π,tht,0,π)</code>
Common display of cone and snail shell	(%i45) <code>wxdraw3d(surface_hide=true,color=green,cone, color=brown,snail)\$</code>

(%t45)



3d-points in the xy-plane, shaping a circle	(%i46) <code>pts:points(makelist([sin(t*%pi/10),cos(t*%pi/10),0],t,1,20))\$</code>
Four vectors, forming a compass rose	(%i47) <code>[v1,v2,v3,v4]:[vector([0,0,1],[0.7,0,0]), vector([0,0,1],[0,0.7,0]),vector([0,0,1], [-0.7,0,0]),vector([0,0,1],[0,-0.7,0])];</code>
	(%o47) <code>[vector([0,0,1],[0.7,0,0]),vector([0,0,1],[0,0.7,0]), vector([0,0,1],[-0.7,0,0]),vector([0,0,1],[0,-0.7,0])]</code>
Texts in three-dimensional space; the text is not aligned to the axes, but to the view direction.	(%i48) <code>text:label(["North",0,1,1],["East",1,0,1], ["South",0,-1,1],["West",-1,0,1]);</code>
	(%o48) <code>label([North,0,1,1],[East,1,0,1],[South,0,-1,1], [West,-1,0,1])</code>
3d-graphic containing points, vectors and texts	(%i49) <code>wxdraw3d(color=red,pts,color=orange, v1,v2,v3,v4,color=blue,text)\$</code>

(%t49)



4.4 General Options

<code>set_draw_defaults(opts,...)</code>	Declares default values for options
<code>terminal=term</code>	output format for the graphic; possible values: screen (default), png, jpg, eps, eps_color, pdf.
<code>file_name="file"</code>	output target for the graphic; default: maxima_out
<code>user_preamble="text"</code>	Gnuplot preamble; contains arbitrary Gnuplot commands, which <i>precede</i> the actual plot process
<code>dimensions=[width,height]</code>	Size of the graphic: in pixels for pixel graphics, in 1/10 mm for vector graphics
<code>columns=n</code>	Number of columns for several scenes in one single graphic
<code>color=colorname</code>	Line color
<code>background_color=name</code>	Background color of the diagram
<code>fill_color=name</code>	Fill color of rectangles, polygons and circles
<code>x(yz)range=[min,max]</code>	Coordinate range of the x(yz)-axis
<code>logx(yz)=true/false</code>	Logarithmic scale of the x(yz)-axis
<code>grid=true/false</code>	Drawing grid lines, if true
<code>x(yz)tics=true/false</code>	Controls the way tic marks are drawn on the x(yz)-axis
<code>x(yz)tics_rotate=true/false</code>	Determines, whether tic marks are rotated by 90°
<code>title="text"</code>	Main title for the scene (default: empty string)
<code>key="text"</code>	Name of a function in the legend (def.: empty string)
<code>x(yz)label="text"</code>	Label for the x(yz)-axis
<code>x(yz)axis=true/false</code>	Determines, whether a x(yz)-axis is to be drawn
<code>x(yz)axis_width=width</code>	Line width of the respective axis
<code>x(yz)axis_color=color</code>	Color of the respective axis
<code>x(yz)axis_type=solid/dots</code>	Line type of the respective axis: solid line (solid) or dotted (dots), default: dots
<code>line_width=width</code>	Line width
<code>line_type=solid/dots</code>	Line type (default: solid)
<code>point_size=size</code>	Point size in point-plots
<code>point_type=n</code>	Point type, possible values: -1,0,1,2,... 13.
<code>points_joined=true/false</code>	Determines, whether points are connected by line segments (default: false)
<code>nticks=n</code>	Number of initial points used by the adaptive plotting routine (default: 30)
<code>adapt_depth=n</code>	Maximum number of splittings used by the adaptive plotting routine (default: 10)

General plot options of the Gnuplot interface *Draw*

`set_draw_defaults` declares default values for arbitrary options, calling that command with an empty parameter list (`set_draw_defaults()`), resets all options to their original default.

Options can be aggregated in *lists*, those lists can be included—even nested—into the parameter list of a plot command in place of single options.

`terminal` and `file_name` declare output format and output target of the graphic. The possible output formats do *not* correspond to the Gnuplot terminals as stated in section 2.2. The file name (default: `maxima_out`) must not have an extension, the appropriate file extension (`.eps`, `.png`, `.jpg`) will be added by Maxima automatically. Unless the path name is given, the file will be saved into the Gnuplot working directory. Declaring `terminal` or `file_name` within the `wx-routines` does not make sense and results in an error message.

The option `user_preamble` can contain any number of Gnuplot commands, separated by semicolons, as a text string. Hence settings can be passed to Gnuplot, which cannot be controlled by plot options (e. g. setting the aspect ratio of a diagram).

The option `dimensions` declares the size of the graphic. The values for height and width do not apply to the diagram, but to the entire graphic (or scene), including labels and margin (default: `[600,500]`).

- Pixel graphics (`png`, `jpg`) are sized in pixels; the same holds true for the `wx-routines` (default: `[500,300]`).
- Vector graphics (`eps`, `jpg`) are sized in 1/10 mm.

Gnuplot preamble, graphic size, color and number of initial points are declared as default values for all subsequent graphics.

```
(%i50) set_draw_defaults(  
      user_preamble="set size ratio -1",  
      dimensions=[200,200],color=red,  
      nticks=200)$
```

Options for suppression of tick marks are put into a list.

```
(%i51) noticks:[xtics=false,ytics=false];  
(%o51) [xtics = false,ytics = false]
```

Generation of a Lissajous curve as a parametric curve

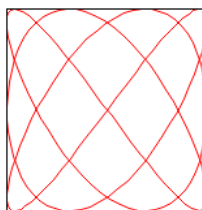
```
(%i52) lissa:parametric(sin(3*t),sin(4*t),t,0,2*%pi);  
(%o52) parametric(sin(3 t),sin(4 t),t,0,2 pi)
```

Drawing the Lissajous curve using the new default options and an additional list of options

```
(%i53) wxdraw2d(lissa,noticks)$
```

><

```
(%t53)
```



Resetting all default values

```
(%i54) set_draw_defaults();  
(%o54) []
```

The option `color` and `fill_color` assign colors to all lines (outlines) and filled shapes, respectively; colors can be declared in hexadecimal form (`#rrggbb`) or by name according to the table below.

`xrange`, `yrange` and `zrange` are the displayed ranges in the respective coordinates in the form `[min,max]`. Their default values are `false`, in that case the displayed range will be calculated

automatically. Setting the `logx`, `logy` and `logz` to `true` causes logarithmic scale of the respective axes.

`grid`, `xtics`, `ytics` and `ztics` control the display of grid lines and tick marks on the axes. `grid=true` causes grid lines to be drawn at the tick marks. The value of `xtics`, `ytics` and `ztics` can be `false` (no ticks), `true` (tick marks calculated automatically) or a *set* of values, at which tick marks (and grid lines, if applicable) are drawn:

```
x(yz)tics={w1,w2,...}
```

Each value can also be a *list* having two elements: a text string, which will be plotted, and a coordinate value for the position of that text string:

```
x(yz)tics={"text1",w1}, {"text2",w2}, ...}
```

The option `x(yz)tics_rotate=true` causes a rotation of the text strings by 90 degree.

`title`, `xlabel`, `ylabel`, `zlabel` and `key` produce labels for the axes and the entire diagram.

	white		light-green		light-pink
	black		dark-green		dark-pink
	gray0		spring-green		coral
	gray10		forest-green		light-coral
	gray20		sea-green		orange-red
	gray30		blue		salmon
	gray40		light-blue		light-salmon
	gray50		dark-blue		dark-salmon
	gray60		midnight-blue		aquamarine
	gray70		navy		khaki
	gray80		medium-blue		dark-khaki
	gray90		royalblue		goldenrod
	gray100		skyblue		light-goldenrod
	gray		cyan		dark-goldenrod
	light-gray		light-cyan		gold
	dark-gray		dark-cyan		beige
	red		magenta		brown
	light-red		light-magenta		orange
	dark-red		dark-magenta		dark-orange
	yellow		turquoise		violet
	light-yellow		light-turquoise		dark-violet
	dark-yellow		dark-turquoise		plum
	green		pink		purple

Farbnamen für das Gnuplot-Interface Draw

Set of values for scale ticks along the y-axis and horizontal grid lines

```
(%i55) yt:setify(create_list(signum(n)
      *sqrt(abs(n)),n,[-4,-3,-1,0,1,3,4])/2);
```

```
(%o55) -1, -1/2, 0, 1/2, 1, -sqrt(3)/2, sqrt(3)/2
```

Values for scale ticks along the x-axis and vertical grid lines as lists, each containing a text string and the x-coordinate

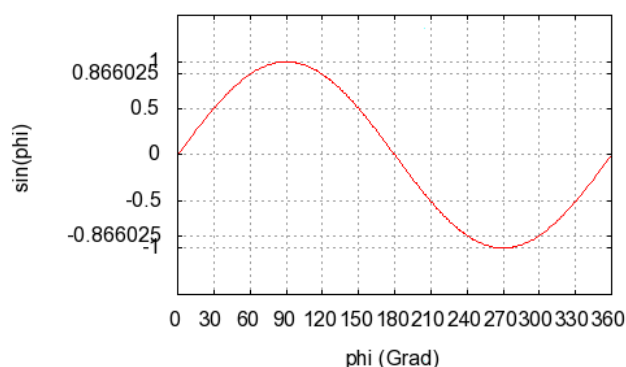
```
(%i56) xt:setify(makelist(
      [string(30*n),30*n*pi/180],n,0,12));
```

```
(%o56) {[0,0],[120,2*pi/3],[150,5*pi/6],[180,pi],[210,7*pi/6],
[240,4*pi/3],[270,3*pi/2],[300,pi/2],[330,5*pi/3],[360,2*pi],
[60,pi/3],[90,pi/2]}
```

Sine curve with gridlines and tick marks

```
(%i57) wxdraw2d(yrange=[-1.5,1.5],xtics=xt,
      ytics=yt,grid=true,color=red,
      explicit(sin(x),x,0,2*pi),
      xlabel="phi (Grad)",ylabel="sin(phi)")$
```

```
(%t57)
```



Point plots (graphic object points) accept the option `point_type` with an integer value between -1 and 16 or a name according to the table below:

-1 \$none	4 square	9 filled_up_triangle
0 dot	5 filled_square	10 down_triangle
1 plus	6 circle	11 filled_down_triangle
2 multiply	7 filled_circle	12 diamant
3 asterisk	8 up_triangle	13 filled_diamant

Possible values of the option `point_type`

Declaring points along a sine curve as a graphic object

```
(%i58) sine:points(float(map(lambda([u],
      [u,sin(u)]),makelist(u,u,-6,6)/2));
```

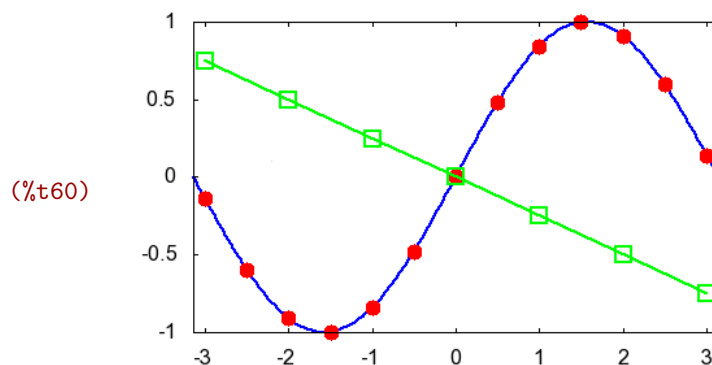
```
(%o58) points([[[-3.0,-0.141],[-2.5,-0.598],[-2.0,-0.909],
[-1.5,-0.997],[-1.0,-0.841],[-0.5,-0.479],[0.0,0.0],
[0.5,0.479],[1.0,0.841],[1.5,0.997],[2.0,0.909],[2.5,0.598],
[3.0,0.141]])
```

Declaring points along a straight line as a graphic object

```
(%i59) line:points(float(makelist([k,-k/4],k,-3,3)));
(%o59) points([[ -3.0,0.75],[ -2.0,0.5],[ -1.0,0.25],[0.0,0.0],
[1.0,-0.25],[2.0,-0.5],[3.0,-0.75]])
```

Sine function and two point plots: Points along the sine function, as well as points along a straight line, connected by line segments.

```
(%i60) wxdraw2d(color=blue,line_width=2,
explicit(sin(x),x,-%pi,%pi),
color=red,point_size=2,point_type=7,
sine,points_joined=true,point_type=4,
color=green,line)$
```



4.5 Options for Labels and Vectors

<code>label_alignment=value</code>	Alignment of the label; possible values: center (default), left, right
<code>label_orientation=value</code>	Orientation of the label; possible values: horizontal (default), vertical
<code>head_length=len</code>	Length of the arrowheads of vectors in units of the x-axis (default: 2)
<code>head_angle=winkel</code>	Angle between arrow heads and segment in degrees (default: 45)
<code>head_type=typ</code>	Type of the arrow head of vectors; possible values: filled (default), empty, nofilled
<code>head_both=true/false</code>	Decides, whether vectors are plotted with two arrow heads

Options for labels and vectors

Three text strings

```
(%i61) [l1,l2,l3]:["left aligned label",
"centered label","right aligned label"]$
```

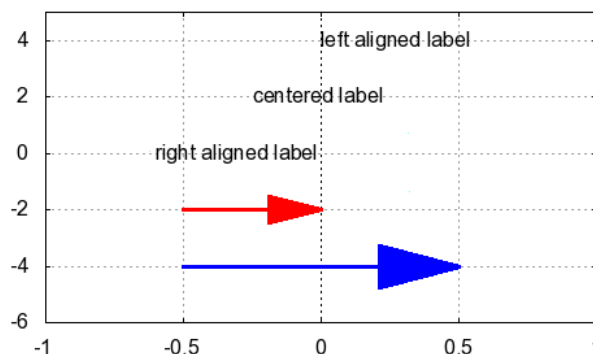
Assigning long option names to short variable names unburdens subsequent writing.

```
(%i62) [la,hs,ha,hl]:[label_alignment,
head_size,head_angle,head_length]$
```

Vectors and variously aligned texts

```
(%i63) wxdraw2d(xrange=[-1,1],yrange=[-6,5],
  yaxis=true,line_width=3,grid=true,la=left,
  label([11,0,4]),la=center,label([12,0,2]),
  la=right,label([13,0,0]),ha=15,h1=0.2,
  color=red,vector([-0.5,-2],[0.5,0]),
  hl=0.3,color=blue,vector([-0.5,-4],[1,0]))$
```

(%t63)



4.6 Options for 2d-Graphics

<code>axis_bottom=true/false</code>	The bottom axis is shown, if true (default).
<code>axis_top=true/false</code>	The top axis is shown, if true (default).
<code>axis_left=true/false</code>	The left axis is shown, if true (default).
<code>axis_right=true/false</code>	The right axis is shown, if true (default).
<code>filled_func=true/false</code>	The area between the plotted function and bottom axis is filled, if true.
<code>filled_func=f</code>	The area between the plotted function and the function f is filled, if true.
<code>transparent=true/false</code>	Polygons are colored according to the option <code>fill_color</code> , if true.
<code>border=true/false</code>	Borders of polygons are painted, if true.

Options for 2d-graphics

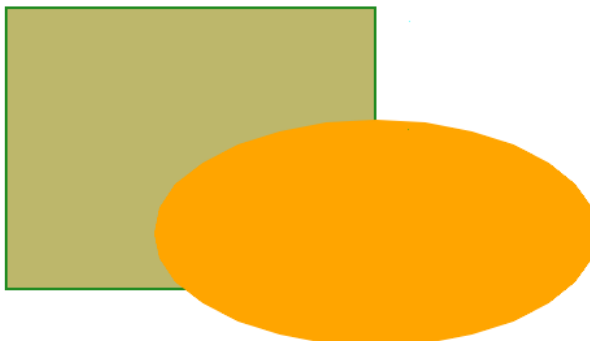
List of options to suppress axes and scale ticks

```
(%i64) noframe:[axis_left=false,axis_right=false,
  axis_top=false,axis_bottom=false,
  xtics=false,ytics=false]$
```

Drawing various shapes with various options

```
(%i65) wxdraw2d(noframe,line_width=2,
fill_color=dark-khaki,
color=forest-green,rechteck,
border=false,fill_color=orange,ell)$
```

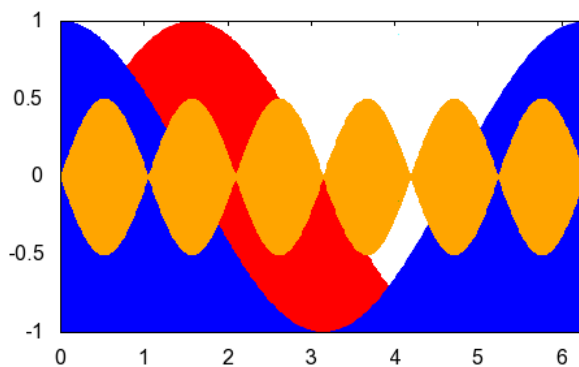
(%t65)



Filling functions with colors

```
(%i66) wxdraw2d(line_width=3,filled_func=true,
color=black,explicit(sin(x),x,0,2*pi),
fill_color=blue,explicit(cos(x),x,0,2*pi),
filled_func=0.5*sin(3*x),fill_color=orange,
explicit(-0.5*sin(3*x),x,0,2*pi))$
```

(%t66)



4.7 Options for 3d-Graphics

<code>view=[φ, ϑ]</code>	Setting the view angle: φ ... around the x-axis, ϑ ... around the z-axis
<code>axis_3d=true/false</code>	Display of all axes in 3d-graphics (default: true)
<code>xu_grid=n</code>	Number of coordinates along the x-axis for drawing grid lines
<code>yv_grid=n</code>	Number of coordinates along the y-axis for drawing grid lines
<code>surface_hide=true/false</code>	Controls the visibility of hidden parts of 3d-surfaces
<code>enhanced3d=true/false</code>	Controls coloring of 3d-surfaces
<code>palette=[r,g,b]</code>	Numbers of the color palettes of the red, green and blue components for image objects and 3d-surfaces
<code>colorbox=true/false</code>	Draws a color scale into the diagram, which uses a color palette, if true (default)
<code>contour=value</code>	Controls contour lines of 3d-surfaces; possible values: none (default), base, surface, both, map
<code>contour_levels=n</code>	n contour lines are drawn at equal intervals.
<code>contour_levels=[x1,dx,x2]</code>	Contour lines are plotted at values from $x1$ to $x2$ with an interval of dx
<code>contour_levels={x1,x2,...}</code>	Contour lines are plotted at the specified levels $x1$, $x2$, etc.
<code>ip_grid=[nx,ny]</code>	Number of initial grid points in implicit plots (default: [50,50])
<code>ip_grid_in=[nx,ny]</code>	Number of secondary grid points in implicit plots (default: [5,5])

Options for 3d-graphics

The option `view=[φ , ϑ]` defines the view on the 3d-graphic with a list containing two elements:

- φ is the rotation around the x-axis in degree; $\varphi = 0$ means horizontal view, $\varphi = 90$ means view from above.
- ϑ is the rotation around the z-axis in degree; $\vartheta = 0$ means front view, $\vartheta = 90$ means view from the side.

`axis_3d` controls the display of all axes in 3d-graphics. To suppress the display of the axes entirely, additional to the option `axis_3d=false` also the tick marks must be turned off using the option `x(xz)tics=false`.

`xu_grid` and `yv_grid` define the number of *coordinates* for grid lines along the x-axis and the y-axis. The number of *grid lines* in the respective direction is by 1 higher than the value of that option. The grid points are connected by line segments. Thus the surface is displayed the more accurately, the higher those values are.

Declaration of a function in two variables

```
(%i67) f:2/(x^2+y^2+1)+1/((x-5)^2+y^2+1);
```

$$(\%o67) \frac{2}{y^2 + x^2 + 1} + \frac{1}{y^2 + (x - 5)^2 + 1}$$

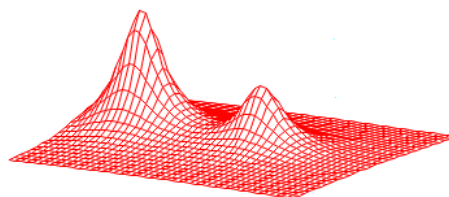
Generation of a graphic object

```
(%i68) g:explicit(f,x,-2,10,y,-6,6)$
```

3D-display of the function

```
(%i69) wxdraw3d(xtics=false,ytics=false,
ztics=false,axis_3d=false,xu_grid=50,
color=red,surface_hide=true,g)$
```

```
(%t69)
```



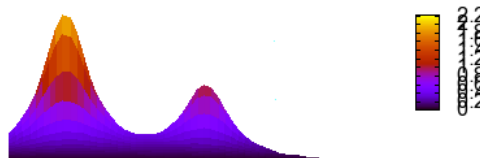
If the option `enhanced3d` is set to `true`, the surfaces are colored with a color gradient, which always depends on the `z`-axis. The color gradient can be defined with the option `palette`. Herein the color function can be selected with a number between 0 and 26, separately for red, green and blue value. The color functions are stated in [1].

The option `colorbox` controls the display of a color scale showing the color gradient.

Function with colored surface. The entire color palette, displayed in a color scale, always fills the entire range of the `z` coordinate, independently of minimum and maximum values of the function.

```
(%i70) wxdraw3d(xtics=false,ytics=false,
ztics=false,axis_3d=false,xu_grid=50,
enhanced3d=true,surface_hide=true,
view=[90,0],g)$
```

```
(%t70)
```

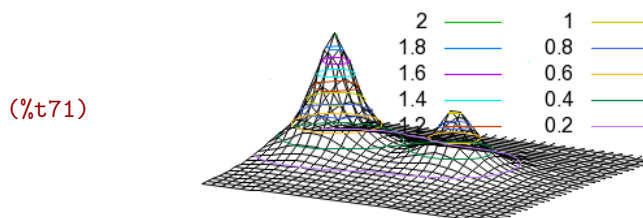


The option `contours` controls the display of contour lines, the following values are possible:

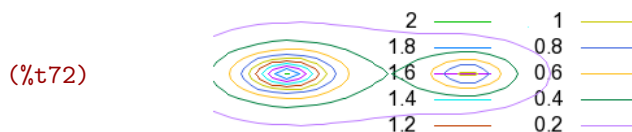
- `none`: No contour lines are drawn (default).
- `base`: Contour lines are projected into the `xy`-plane.
- `surface`: Contour lines are drawn on the surface.
- `both`: Contour lines are drawn both in the `xy`-plane and on the surface.
- `map`: View from above (corresponds to `rot_vertical=0`), grid lines are not displayed.

The option `contour_levels` declares the number and the values of contour lines.

Display of contour lines on the surface `(%i71)` `wxdraw3d(xtics=false,ytics=false,ztics=false,axis_3d=false,contour_levels=10,contour=surface,g)$`



Displaying the function as contour plot `(%i72)` `wxdraw3d(xtics=false,ytics=false,ztics=false,axis_3d=false,contour_levels=10,contour=map,g)$`



Bibliography

- [1] Maxima Development Team: *Maxima Reference Manual V.5.23*. 2011.
- [2] Philipp K. Janert: *Gnuplot in Action, Understanding Data with Graphs*. Manning Publications 2009.
- [3] Mario Rodríguez Riotorto: *A Maxima-Gnuplot Interface*.
<http://www.telefonica.net/web2/biomates/maxima/gpdraw>.